

**Problem 1**

The charge  $Q_S$  of an ultrafast (delta-like) current pulse signal is acquired using the circuit shown in the figure where  $C = 10\text{pF}$ . The preamplifier features an input impedance  $R_{i,A} = 10\text{M}\Omega$ , two input-referred noise generators with unilateral spectral density  $\sqrt{S_V} = \frac{10\text{nV}}{\sqrt{\text{Hz}}}$ ,  $S_i = \frac{0.1\text{pA}}{\sqrt{\text{Hz}}}$ , and its bandwidth is limited by a single pole at  $f_A = 200\text{MHz}$ .

- 1) Calculate the minimum charge  $Q_S$  that could be ideally measured using an optimal filter. Then evaluate the minimum charge that can be obtained replacing the matched filter with a sampler at the frequency of  $10\text{MHz}$  and applying a suitable digital filtering.
- 2) Calculate the minimum charge  $Q_S$  that could be measured if the sample&hold of the sampler of point 1) is replaced with a gated integrator featuring an integration window of duration  $T_G = 10\text{ns}$  (i.e. the signal is sampled multiple times, each sample is obtained integrating for an interval  $T_G=10\text{ns}$ ).
- 3) Compare from a theoretical point of view the filtering action that can be obtained using a boxcar integrator and the one achievable using a ratemeter integrator.

**Problem 2**

We want to detect the optical signal emitted by a sample excited by a laser. The sample is excited at a frequency of  $10\text{MHz}$  and it emits an exponential optical signal with a decay time of  $4\text{ns}$  at a wavelength of  $800\text{nm}$ . The current signal produced by a photodetector is collected using a  $10\text{-k}\Omega$  resistor followed by an amplifier featuring a large bandwidth limited by a single pole at  $500\text{MHz}$  and input-referred noise with unilateral spectral density having a wideband component ( $\sqrt{S_V} = \frac{10\text{nV}}{\sqrt{\text{Hz}}}$ ) and  $1/f$  noise component with frequency  $f_c=2\text{kHz}$ . An optical bandpass filter with a narrow bandwidth centered at  $800\text{nm}$  is exploited. Nevertheless, a residual background of  $10^4\text{ ph/s}$  at  $800\text{nm}$  reaches the photodetector.

- 1) Considering the exploitation of a silicon photodiode, define the characteristics that you consider reasonable for the detector in this application. Design a suitable filtering scheme and calculate the minimum detectable optical power of the signal.
- 2) Evaluate how the answer to the previous point would change if a silicon APD were available.
- 3) Compare silicon APD detectors and PMTs from a theoretical point of view.

