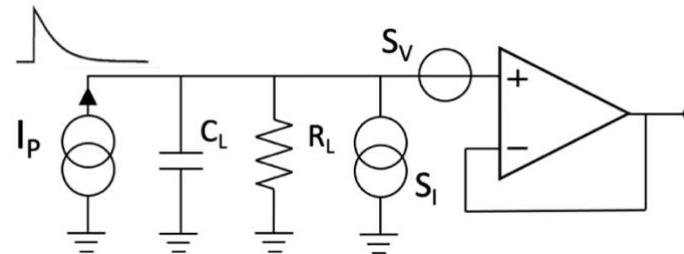


Problem 1

As sketched in the figure below, a current signal is acquired by a preamplifier featuring a very high input impedance (of the order of $1\text{ G}\Omega$), a band limited by a single pole at a frequency $f_P = 200\text{ MHz}$ and two input-referred noise generators with unilateral spectral densities $(S_V)^{1/2} = 1\text{ nV}/(\text{Hz})^{1/2}$ and $(S_I)^{1/2} = 1\text{ pA}/(\text{Hz})^{1/2}$. $C_L = 2\text{ pF}$ and $R_L = 10\text{ M}\Omega$ represent the total capacity and resistance, respectively, between the sensor output and ground. The detector delivers trains of exponential pulses with unknown amplitude A_P , decay time constant $T_P = 20\text{ ns}$ and repetition rate $r_P = 1\text{ kHz}$. The duration of the measurement can span from 1 to 20 min.

- 1) Describe in detail how you can calculate the **optimum filter** and **calculate the minimum amplitude** that could be detected for each single pulse.
- 2) Considering now that the amplitude of the pulses slowly changes with a timescale of 1s, **design a suitable filter** to exploit this new information and **calculate the minimum detectable signal amplitude** with the proposed solution.
- 3) Considering now that the current noise of the preamplifier has also a $1/f$ component with $f_c = 50\text{ kHz}$, evaluate its effect on the measurement in the conditions of point 2). Then provide a solution to limit its effect and **calculate the minimum detectable signal amplitude** with the proposed solution.

**Problem 2**

Samples of a fluid flowing inside a capillary at a speed of 20 cm/s are analyzed. We want to detect with $S/N > 10$ the presence of any micro-bubble whose size is $1\text{ }\mu\text{m}$. To do this, a continuous wave laser emitting at 800 nm and a silicon APD are used to measure the light reflected by the fluid within the capillary. Each sample is analyzed in about 30 minutes. The fluid reflectivity is 5% while the bubble one is 6%. The light coming from the capillary is focused on a small spot of the APD ($\ll 1\text{ }\mu\text{m}$). The detector features $G=200$, $F=2$, a dark current rate of 1000 electron/s and it is connected to a transimpedance amplifier having total wideband noise referred to the input with unilateral spectral density $\sqrt{S_{I,U}} = 0.1\text{ pA}/\sqrt{\text{Hz}}$.

- 1) Choose a reasonable detection efficiency of the APD and describe a suitable acquisition scheme. Motivate your answer and **calculate the minimum laser optical power** necessary to achieve the desired S/N . Consider the bubble like a square of different reflectivity.
- 2) Discuss how would you change the answer to point 1) if the **fluid speed is reduced to $200\text{ }\mu\text{m/s}$** . Calculate the minimum necessary laser optical power in this new scenario.
- 3) In the conditions of point 2), consider now also the presence of a **$1/f$ noise component** of the amplifier with **$f_c = 2\text{ kHz}$** . Calculate the minimum necessary laser optical power with and without a modulation of the laser.