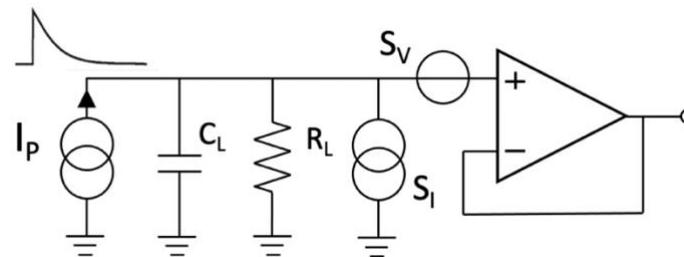


Problem 1

As sketched in the figure below, a current signal is acquired by a preamplifier featuring a very high input impedance (of the order of 1 GΩ), a band limited by a single pole at a frequency $f_P = 200$ MHz and two input-referred noise generators with unilateral spectral densities $(S_V)^{1/2} = 1$ nV/(Hz)^{1/2} and $(S_I)^{1/2} = 1$ pA/(Hz)^{1/2}. $C_L = 2$ pF and $R_L = 10$ MΩ represent the total capacity and resistance, respectively, between the sensor output and ground. The detector delivers trains of exponential pulses with unknown amplitude A_P , decay time constant $T_P = 20$ ns and repetition rate $r_P = 1$ kHz. The duration of the measurement can span from 1 to 20 min.

- 1) Describe in detail how you can calculate the **optimum filter** and **calculate the minimum amplitude** that could be detected for each single pulse.
- 2) Considering now that the amplitude of the pulses slowly changes with a timescale of 1s, **design a suitable filter** to exploit this new information and **calculate the minimum detectable signal amplitude** with the proposed solution.
- 3) Considering now that the current noise of the preamplifier has also a 1/f component with $f_c = 50$ kHz, evaluate its effect on the measurement in the conditions of point 2). Then provide a solution to limit its effect and **calculate the minimum detectable signal amplitude** with the proposed solution.



Problem 2

Samples of a fluid flowing inside a capillary at a speed of 20cm/s are analyzed. We want to detect with $S/N > 10$ the presence of any micro-bubble whose size is 1μm. To do this, a continuous wave laser emitting at 800nm and a silicon APD are used to measure the light reflected by the fluid within the capillary. Each sample is analyzed in about 30minutes. The fluid reflectivity is 5% while the bubble one is 6%. The light coming from the capillary is focused on a small spot of the APD ($\ll 1$ μm). The detector features $G = 200$, $F = 2$, a dark current rate of 1000electron/s and it is connected to a transimpedance amplifier having total wideband noise referred to the input with unilateral spectral density $\sqrt{S_{I,U}} = 0.1$ pA/ \sqrt{Hz} .

- 1) Choose a reasonable detection efficiency of the APD and describe a suitable acquisition scheme. Motivate your answer and **calculate the minimum laser optical power** necessary to achieve the desired S/N. Consider the bubble like a square of different reflectivity.
- 2) Discuss how would you change the answer to point 1) if the **fluid speed is reduced to 200μm/s**. Calculate the minimum necessary laser optical power in this new scenario.
- 3) In the conditions of point 2), consider now also the presence of a **1/f noise component** of the amplifier with **$f_c = 2$ kHz**. Calculate the minimum necessary laser optical power with and without a modulation of the laser.