

Problem

A portable sensor system emits a double rect signal having the shape shown in Figure, with $T_P = 10\text{ms}$, $T_W = 20\text{ms}$ and a variable amplitude V_P . The system preamplifier bandwidth is 100 MHz and its input-referred noise generator features an **unilateral** spectral density $\sqrt{S_V} = 10\text{nV}/\sqrt{\text{Hz}}$ and $1/f^2$ noise component with $f_c = 10\text{kHz}$. An auxiliary signal synchronous to the signal of interest is provided with a high SNR. The maximum duration of the measurement with this system is 1 hour.

- 1) Describe in detail how you can calculate the **optimum filter** and evaluate the minimum detectable signal with this filter.
- 2) In the same conditions of point 1), consider now the possibility of replacing the **matched** filter with an analog or a digital filter.
 - In the analog approach, it is possible to use only a **SINGLE** gated integrator: choose the filter parameters and calculate the minimum detectable signal amplitude.
 - In the digital approach, it is possible to use a maximum sampling frequency of 100kHz. Discuss the guidelines to design a digital filter and provide the expression of the resulting signal to noise ratio (SNR).
- 3) Considering now also the presence of $1/f^3$ noise with $f_c = 2\text{kHz}$ at the output of the sensor, evaluate the effect of this noise on the measurement. Considering **only the analog approach**, discuss qualitatively how it would be possible to modify the filtering scheme to minimize its effect.

