

(NB: see text also on the other side of the sheet)

### Problem 1

#### Signal

Rectangular pulses

Amplitude:  $V_P$  (variable)

Duration:  $T_P=100\mu s$

Repetition rate: 100Hz

#### Noise

$S_V^{1/2} = 10nV/Hz^{1/2}$  white noise spectral density (unilateral)

$B/f^2$  component, with  $f_c=20kHz$

$f_{pa} = 10 MHz$  upper band-limit of the preamplifier

The time-varying amplitude  $V_P$  of a sequence of rectangular pulses of duration  $T_P$  is to be measured for each pulse individually. The signal is read-out by a preamplifier and the total noise superimposed to the signal consists of a wideband component and a  $B/f^2$  component as above specified.

- A) Evaluate the minimum measurable amplitude  $V_{P,MIN}$  without using any additional filter. Then, describe and explain the ideal filter that makes it possible to measure the pulse amplitude  $V_P$  with the best possible Signal-to-Noise ratio and evaluate the minimum amplitude  $V_{P,MIN}$  thus measurable.
- B) Select a suitable practical filter that is a good approximation of the optimum filter for this signal, select the filter parameters and evaluate the minimum amplitude  $V_{P,MIN}$  that can be measured in these conditions. Consider that a sync signal can be provided with the signal, if needed.
- C) Consider now the exploitation of a fully digital approach to approximate the optimum filter. Discuss the guidelines to select the sampling frequency and how this choice could have an impact on the Signal-to-Noise ratio. Choose a reasonable value for the sampling frequency and evaluate the minimum amplitude  $V_{P,MIN}$  that can be measured in this case.
- D) Consider now an additional **1/f noise component superimposed to the two noise components** considered so far. Evaluate the maximum corner frequency of the 1/f component that can be tolerated to guarantee a negligible impact of the 1/f noise.

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## Problem 2

<b>STRAIN GAUGE</b> $R=300\Omega$ $G=2$ ; Max. Power= $3\mu\text{W}$	<b>PREAMPLIFIER</b> $S_{vA} = 10nV/\sqrt{Hz}$ $f_{pA} = 1MHz$
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A metal bar is subject to both compression/extrusion and bending strain. We want to measure only the compression/extrusion strain. To carry out this measurement we have strain gauges with the characteristics reported above.

- A) Considering the exploitation of only **two** strain gauges, draw the configuration that you would use to achieve the goal. Provide a quantitative explanation of your design.
- B) Evaluate the maximum temperature variation that can be tolerated to have a sensitivity of 50microstrain. Consider a typical temperature dependence for the strain gauges. Discuss if and how it is possible to mitigate this issue if more than two strain gauges can be exploited.
- C) Describe into details the weighting function in the time domain and the frequency behavior of a lock-in amplifier with a sinusoidal reference and with a square wave reference.
- D) Consider now that the preamplifier is affected by an additional 1/f noise component with a corner frequency  $f_C=5kHz$ . Provide a quantitative evaluation of the sensitivity that can be achieved exploiting the two filters discussed in C).